Combinatorics

- 1. In how many different ways can a 3-person committee be selected from 6?
- 2. In a 7 horse race, Bill thinks horses 1, 4, 6 will be the top 3 horses in the race, but not necessarily in that order. If Bill is correct, how many different outcomes are possible?
- 3. A committee of 3 students is to be selected from a group of 10 to be on a committee to plan a school trip. How many different committees can be selected?
- 4. In a regular heptagon ABCDEFG, how many triangles can be constructed whose vertices are among the points A, B, C, D, E, F, and G?
- 5. How many different 3-letter "words" are possible such that the letters of each word are in alphabetical order? (For example, the "word" ADF is in alphabetical order.)
- 6. 3 pennies are to be placed onto a 5 b y 5 grid. How many ways can you place the 3 pennies such that non of them share the same row or column?
- 7. An election has three different positions: President, Vice President, and Secretary. There are 4 people running for President, 3 for VP, and 5 for Secretary. If a person is voting on a ballot, how many ways can someone fill in the ballot. Assume that you can not submit an empty ballot.
- 8. How many ways can 5 people A, B, C, D and E sit in a row if A must be to the left of B but not necessarily next to each other?

- 9. How many ways can 3 boys and 3 girls sit in a row if:
 - a. There are no restrictions on where they sit in the row?
 - b. All the boys sit together, and all the girls sit together?
 - c. Only the boys must sit together, the girls choosing the other seats?
- 10. A committee consists of 4 men and 2 women. A subcommittee is to be formed consisting of 1 man and 1 woman. In how many different ways can the subcommittee be formed?
- 11. There are 8 boys and 12 girls in a class. A team of 5 is to be formed with 3 girls. How many different teams are possible?
- 12. There are 8 boys and 12 girls in a class. A team of 5 is to be formed with 3 girls. If the teams must have at least 2 boys, how many different teams are possible?
- 13. Three boys and their girlfriends have 6 seats at a hockey game. In how many ways can they be seated if each couple must sit together?
- 14. There are ten teams in a school district competition. Each team plays each other team once. What is the total number of games played in the competition?
- 15. An intramural league has 4 teams. If each team is scheduled to play each of the remaining teams exactly twice during the season, how many games are scheduled
- 16. If there are 8 people in a room and each person shakes every other person's hand once, how many handshakes will there be?
- 17. Nine people apply for a job in which 2 people are selected to work in an office and 3 in the workyard. In how many different ways can the selection be made?